

Depth of Induction of the Equatorial Electrojet in the African Region using Solar Quiet (Sq) Field Variation

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ABSTRACT

The depth of induction of the Equatorial electrojet current to electrical conductivity of the subsurface of the solid earth in the region of Africa was determined using naturally geomagnetic variation on quiet days generated by fluctuating electric current in the ionosphere. The study used magnetic data collected from records of magnetic observatories located in the region of Africa: Ilorin (4.68°N, 8.50°E), Addis Ababa (9.04°N, 38.77°E), Algeria (36.85°N, 2.93°E) and Khartoum (15.33°N, 32.32°E) acquired by SuperMag magnetic data centre in the year 2011. The EEJ strength was estimated by subtracting variation in horizontal component geomagnetic field of stations located off the EEJ strip from the daily variation in horizontal component of stations located within the EEJ strip. The internal and external field contributions to the variations in Sq(H) was separated using spherical harmonics analysis (SHA). A transfer function was employed in estimating the conductivity-depth profile for the external and internal paired coefficients of the Spherical Harmonics Analysis (SHA). The electrojet current was observed to penetrate the lower mantle to depth of about 1092km in the African region. The conductivity-depth structure was observed to increase downward with a high conductivity observed within depth of 116km and 326km, which is likened to seismic low velocity region. Findings also reveal conductivities to be below 1.5S/m below 600km increasing up to about 2S/m at the lower mantle.

Keywords: Induction, Equatorial, Electrojet, African Region, Solar Quiet, Field Variation

INTRODUCTION

The variation of the magnetic field of the earth has large spectrum coverage and period that ranges from few seconds to millions of years [1,2]. The variations that take place over a period of years are called geomagnetic secular changes and are known to have their origin in the earth's outer core. The changes in the earth's magnetic field that are short termed are known as transient variation and have their origin from currents flowing in the ionosphere and the magnetosphere according to [3,4]. Currents flowing in the magnetosphere and ionosphere causes geomagnetic storms and substorms. The changes in the earth's magnetic field observed on magnetic quiet days are the smoothest and most regular and are known as solar quiet (Sq) daily variations [5]. Solar quiet daily variation is one of the transients geomagnetic changes attributed to solar events and other number of related phenomena of the upper atmosphere [6]. [7] showed that an abnormally large daily

variation usually two or three fold enhancement in Sq (H) occurs within a narrow range of dip latitude centered over the magnetic equator within a narrow belt of latitudes ($\pm 3^\circ$ over the dip equator), and was named Equatorial Electrojet. [8] pointed out that an east-ward current flowing in the E-region of the ionosphere causes the electrojet. The electrojet strength in a given location is computed by subtracting the daily variation of X or H component of the earth's magnetic field at off equatorial stations from the daily variation of H or X component of the geomagnetic field at the equatorial (EEJ) station, in the same longitudinal zone. The enhancement in the Sq (H) daily variation in the earth's magnetic field observed at equatorial stations are of great significance. This is due to its close association with solar weather condition. According to Baker and Martyn 1953, a huge east-ward conductivity due to the electric and magnetic field intersecting at

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right angle at the dip equator, is the cause of the equatorial electrojet current with the normal Sq electric field [9]. The flowing current in the ionosphere induces magnetic perturbation on the ground. The nature of the head currents together with the spread of electrically conducting materials in the solid earth, determines the extent of penetration, magnitude as well as the direction of the induced current. Magnetometers in geomagnetic observatories on the earth surface record a hybrid of the head current (external) and the induced (internal) field parts of the currents. The conductivity of the solid earth can be obtained by separating the external (head) current and the induced internal current into their separate parts with the help of spherical harmonic analysis technique and other techniques according to [10]. The conductivity -depth structure of the solid earth has been obtained in time past using different geophysical methods amongst them are; seismic, gravity, resistivity methods, aeromagnetic techniques. Older workers including [11,12,13] noted that these methods are limited to depth of 200 Km from the earth crust. The large physical energy required and the complications involved in these techniques were also emphasized. The integration of the upper atmosphere with the solid Earth using slowly naturally time varying geomagnetic

In this work, geomagnetic data recorded by magnetometers in observatories installed in Africa (Ilorin (4.68° N, 8.50° E), Algeria (36.85°N, 2.93°E), Addis Ababa (9.04°N, 38.77°E) and Khartoum (15.33°N, 32.32° E) acquired by Supermagnetic data center for

Four stations in the African region were used for the purpose of the study. Two of the stations are off the equatorial electrojet influence (latitude $\pm 3^\circ$ over the equator) which are Medea (AO₂) in Algeria and Khartoum in Sudan (KRT). The other two stations are within the influence of the

Ese and Obiekezie field arising from unsteady currents in the upper atmosphere is known to be a useful tool in profiling the conductivity -depth structure of the deep earth to greater depth. The current derived from changes in the earth's magnetic field obtained from a long period of geomagnetic variation can be used to investigate the conductivity of the earth to a depth range of 200- 1500 km according to [11]. Previous works on profiling conductivity depth structure in Africa including the work of [14,15] have used Sq current in profiling conductivity depth structure in the African region. They found intriguing results that have helped in understanding the solid Earth interior. For example [16], worked in the African region and found conductivity that increases downwards. They reported a high conductivity at depth of 100km and 205 km corresponding to seismic low velocity region. Also, [16] worked in Malaysia. They determined the mantle electrical conductivity depth structure of Malaysia using Sq currents. They reported a conductivity that increases downwards. The aim of this work was to extract the narrow band electrojet current from the Worldwide Sq in the African region to profile the depth of induction of the equatorial electrojet current to subsurface conductivity in the African region using natural geomagnetic variation.

Data Source

the year 2011 were used. The stations include two stations within the influence of the EEJ (Ilorin and Addis Ababa) and two stations outside the EEJ influence which are Algeria and Khartoum.

Stations under study

equatorial electrojet current: Ilorin in Nigeria (ILR) and Addis Ababa (AAE) as shown in Fig 1 below. The thick line in Fig 1 represents the equator. The geographic and geomagnetic coordinates of the stations and their code are in Table 1 below.

Table 1 Stations and their coordinates.

s/n	Station	Code	Country	GeogrLat	Geographic Longitude	Geomagnetic Latitude	Geomagnet Long
1	Ilorin	ILR	Nigeria	8.50	4.68	-1.25	76.73
2	Algeria	AO2	Algeria	36.85	2.93	27.98	77.67
3	AddisAbaba	AAE	Ethiopia	9.04	38.77	0.77	110.94
4	Khartoum	KRT	Sudan	15.33	32.32	5.69	103

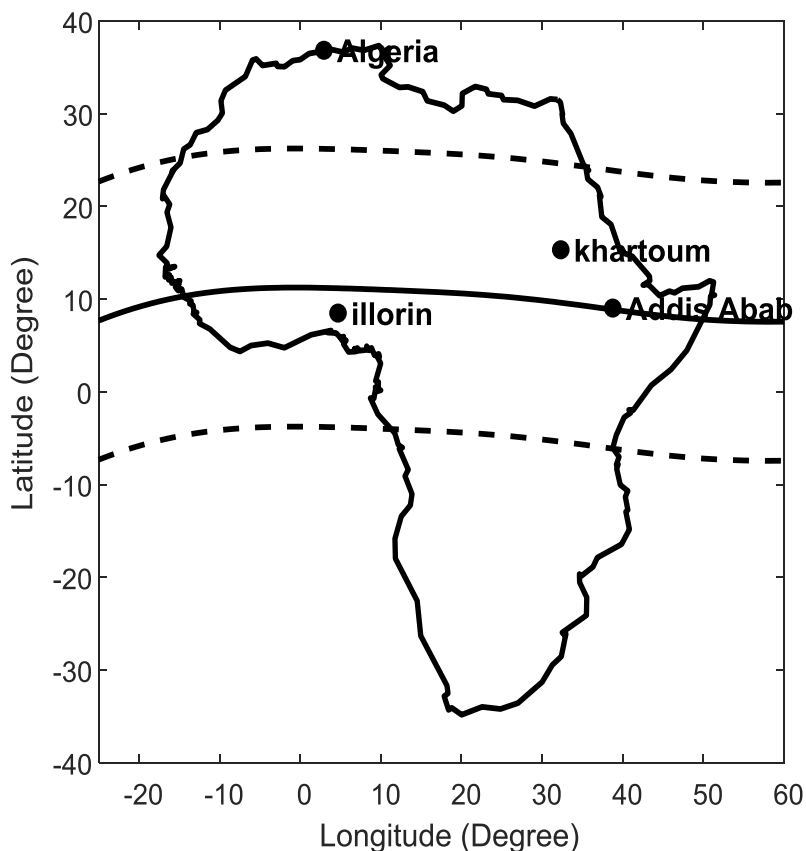


Fig 1: Geographical map of the stations
Method of Data Analysis

First, magnetically quiet days was selected using the 2011 planetary geomagnetic disturbance K_p index. The maximum value for each day of 2011 was used to select five magnetically quiet days in each month of the year, making a total of sixty quietest days as shown in Table 1. The five quietest days used were those which have the greatest value of the planetary geomagnetic disturbance index is less than or equal to 2. The data used were minute by minute data which were converted to hourly value (24hrs) for each of the five selected days. The hourly value for each of

the five selected quiet days were summed up and their average calculated. The result is the 24-hourly average for each month of the year for the horizontal component of the geomagnetic field. The mean values of horizontal component of the geomagnetic field of the four hours flanking midnight were used as the baseline in this work. The hourly departure from the midnight baseline was computed for the horizontal component geomagnetic field and non-cyclic variation to obtain the solar quiet daily variation in the horizontal component geomagnetic field $Sq(H)$ shown in Table 3a-

b. The EEJ strength was obtained by subtracting solar quiet variation in horizontal component of the geomagnetic field at a station off the EEJ influence from a station within the EEJ strip. The two stations must lie in the same or close longitude in accordance with [17]. Spectral (Fourier) analysis was carried out obtaining spectral analysis (4 harmonics) of each Fourier (sine and cosine) coefficients for the year under study (2011). Thereafter, spherical harmonic analysis (SHA) was

$$C_n^m = z - ip \tag{1}$$

“This forms a complex number in which the real (z) and the imaginary (-p) parts are given by” [6]:

$$z = \frac{R}{n(n+1)} \left\{ \frac{A_n^m [na_n^{me} - (n+1)a_n^{mi}] + B_n^m [nb_n^{me} - (n+1)b_n^{mi}]}{(A_n^m)^2 + (B_n^m)^2} \right\} \tag{2}$$

$$p = \frac{R}{n(n+1)} \left\{ \frac{A_n^m [nb_n^{me} - (n+1)b_n^{mi}] - B_n^m [na_n^{me} - (n+1)a_n^{mi}]}{(A_n^m)^2 + (B_n^m)^2} \right\} \tag{3}$$

where R is the Earth’s radius in km, z and p are given in km and the coefficient sums are also given by the equation $a_n^{me} + a_n^{mi} = A_n^m$ and $b_n^{me} + b_n^{mi} = B_n^m$.

The depth to substitute layer in km for each pair of coefficients is given by :

$$d_n^m = z - p \cdot \sigma_n^m = \frac{5.4 \times 10^4}{m(\pi p)^2} \text{ S/m}$$

Ese and Obiekezie carried out, obtaining the Legendre polynomial external and internal coefficients. [18], devised a means of computing the depth (d) in km to equivalent layer of conductivity(σ) in S/m, that can produce the observed field measurement at the Earth surface for each SHA coefficients of degree n and order m. Campbell and Anderssen (1983) generalized this form and [19] modified this as:

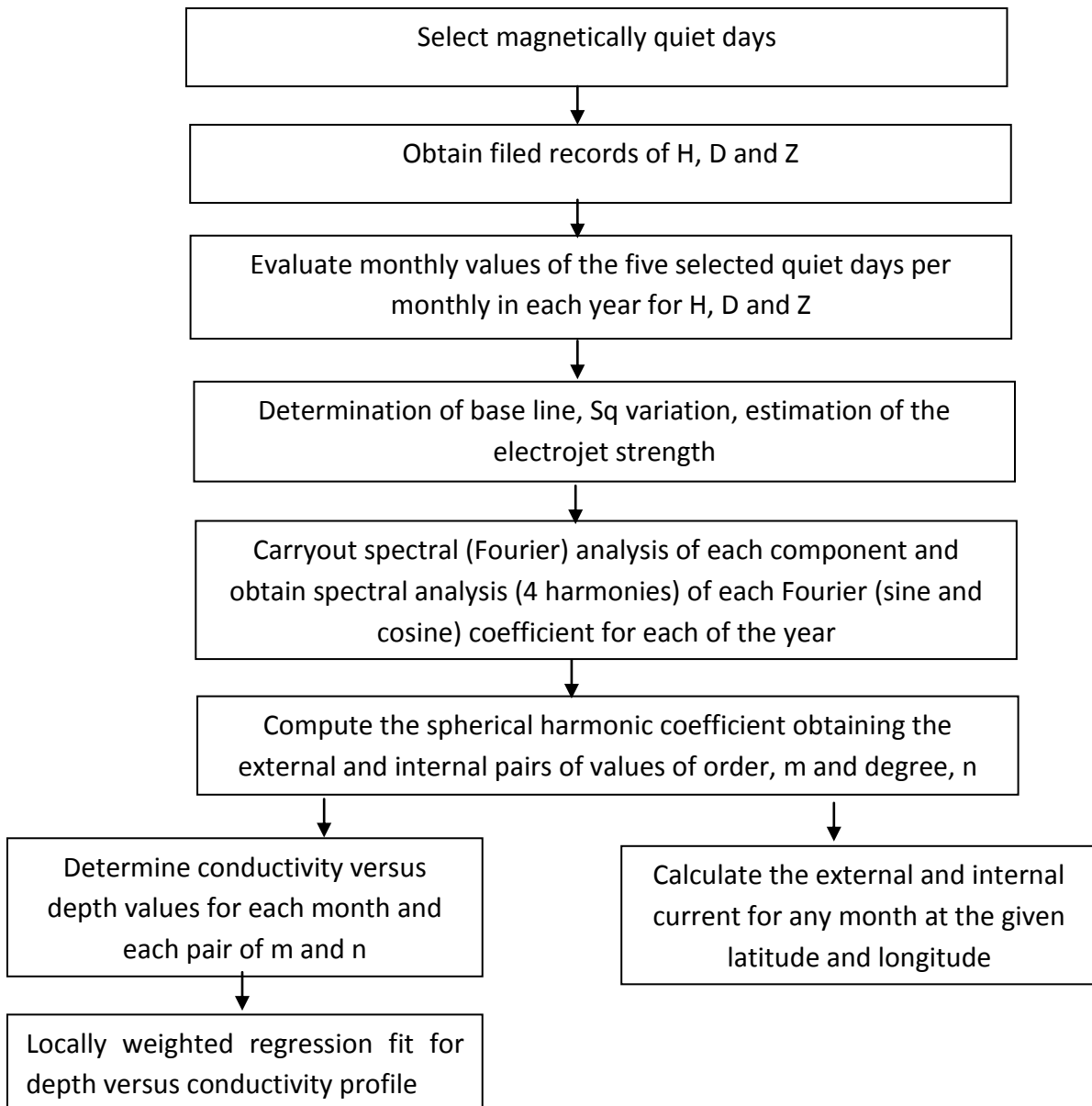


Fig 2: Data processing flow chat

RESULTS AND DISCUSSION

Table 1: Geomagnetic quiet days and their K_p values for 2011

Jan	23	30	5	27	21
K_p	0	0	1	1+	2-
Feb	3	9	27	13	28
K_p	0+	1	1	1	1
Mar	15	26	16	18	27
K_p	0+	0+	1-	1	1
Apri	26	27	10	16	26
K_p	1-	1-	1	1	1+
May	20	8	15	12	9
K_p	1-	1	1	1+	1+
Jun	29	3	19	27	28
K_p	1-	1	1+	2-	2-
Jul	27	28	16	24	17
K_p	1+	1+	1+	1+	2-
Aug	31	3	18	19	21
K_p	1-	1	1	1	1+
Sept	23	16	19	1	8
K_p	1-	1	1	1+	2-
Oct	28	29	22	14	23
K_p	0+	0+	1-	1-	1
Nov	14	19	9	20	13
K_p	0+	0+	1-	1-	1
Dec	27	16	26	17	6
K_p	0	0+	0+	1-	1-

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10.67628	43.36526	15.39026	69.38563	67.32307	11.806304	58.11799	55.89476	93.11904	13.12209	48.70167	59.24894	90.85367	4.253239	49.76378	60.50765	77.83233	-0.986391	47.456	48.63926	73.70415
11.71785	36.39378	22.18352	57.86989	55.1402	17.042913	51.21147	39.76102	72.17513	10.53003	35.24602	43.5618	69.05402	1.455283	39.20135	45.47096	60.65398	-3.789174	33.632	31.62778	61.32046
8.571413	28.0803	21.37478	38.17415	33.46733	15.039522	38.40995	23.44728	52.84322	3.600462	22.32037	29.19467	51.37437	5.405804	26.75491	32.03426	50.13363	-5.655957	23.198	19.6363	44.55476
1.688978	21.50083	15.70404	16.82441	15.59046	11.18613	24.07342	11.55104	36.1373	-0.4641	12.88872	19.16754	34.38672	5.522326	17.51848	23.17957	37.98528	-6.340739	12.17	12.65483	30.08507
-5.03746	13.29135	8.297299	5.884674	6.489587	4.928739	10.8619	4.699799	22.70539	-2.68617	5.535065	15.09441	21.60507	5.610848	10.35204	17.83487	24.58494	-5.801522	4.194	8.761348	16.65737
-7.70789	6.84987	2.76256	2.400935	3.992717	1.233348	1.69538	3.97106	12.17548	-1.24573	2.481413	12.17928	11.48941	-3.21937	7.545609	11.81217	16.01459	-2.648304	1.34	6.84187	11.23767
-5.57833	0.118391	1.329821	1.307196	0.317848	0.213957	-3.85114	1.182321	4.657565	1.557201	1.531761	7.344152	3.307761	0.115891	5.803174	5.433478	8.906239	-0.743087	1.756	4.040391	7.167978
-2.82876	-3.53709	1.019082	-0.09254	-1.96302	0.246565	-4.88266	-1.32642	-0.49435	0.775136	0.378109	4.945022	0.016109	0.389587	2.806739	2.982783	4.379891	-0.64787	0.926	2.056913	4.590283
-2.0972	-2.65257	1.236342	-0.77228	-1.40589	-0.224826	-1.27419	-3.03016	-0.07626	-1.36443	-0.72754	3.323891	-0.63154	0.545065	0.162304	1.692087	1.639543	-0.802652	-0.43	0.787435	2.629087
-2.82963	-1.72804	2.053603	-0.39602	-1.55476	-1.704217	-3.06571	-3.9289	-1.45817	-0.574	-2.4252	1.848761	-1.2552	1.314543	-1.20013	0.411391	-0.6068	-1.103435	-1.728	-0.36004	1.171391
-3.78407	-1.22752	0.348864	-1.36376	-2.12963	-2.099609	-4.40723	-4.07014	-2.74609	-0.04356	-3.79685	-0.24437	-2.85085	1.612022	-1.74857	-0.8813	-1.35115	-1.102217	-2.412	-1.57352	-0.8938
-2.3625	-0.403	-0.24988	-2.0375	-2.1825	-2.231	-6.43875	-4.92138	-3.636	-0.32813	-3.8645	-2.3935	-4.4685	0.7235	-1.515	-1.35	-1.5955	-1.793	-3.014	-2.611	-1.5615

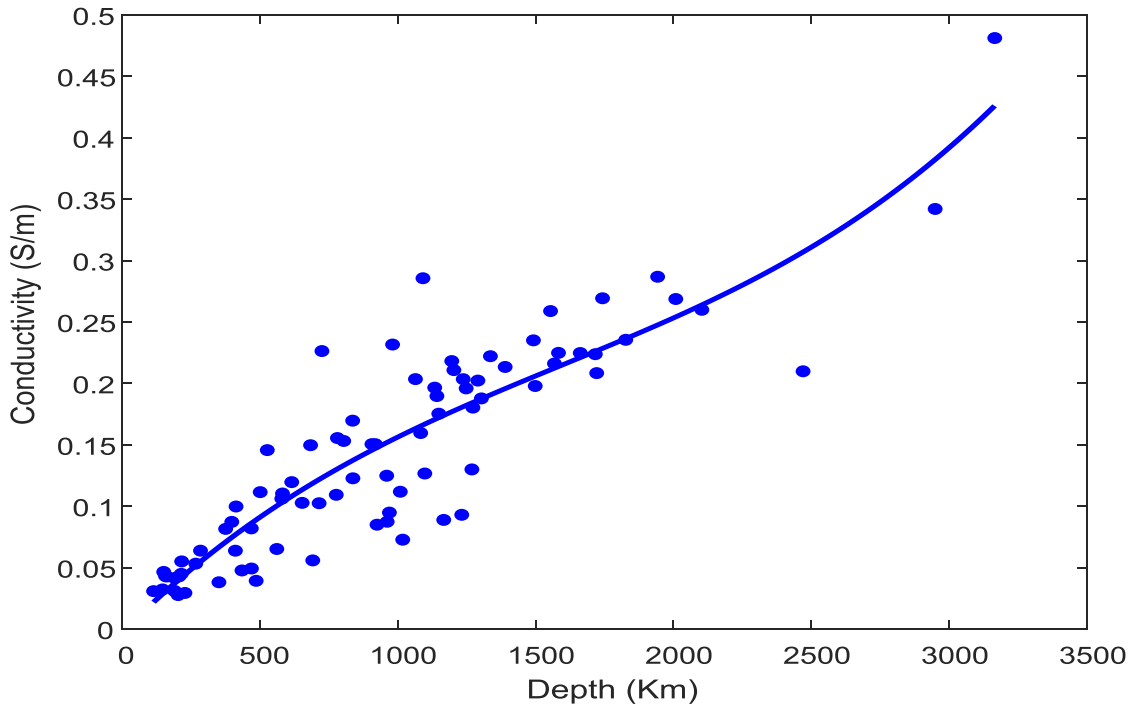


Fig 3: Depth of induction of EEJ to subsurface electrical conductivity for Ilorin/Algeria pair

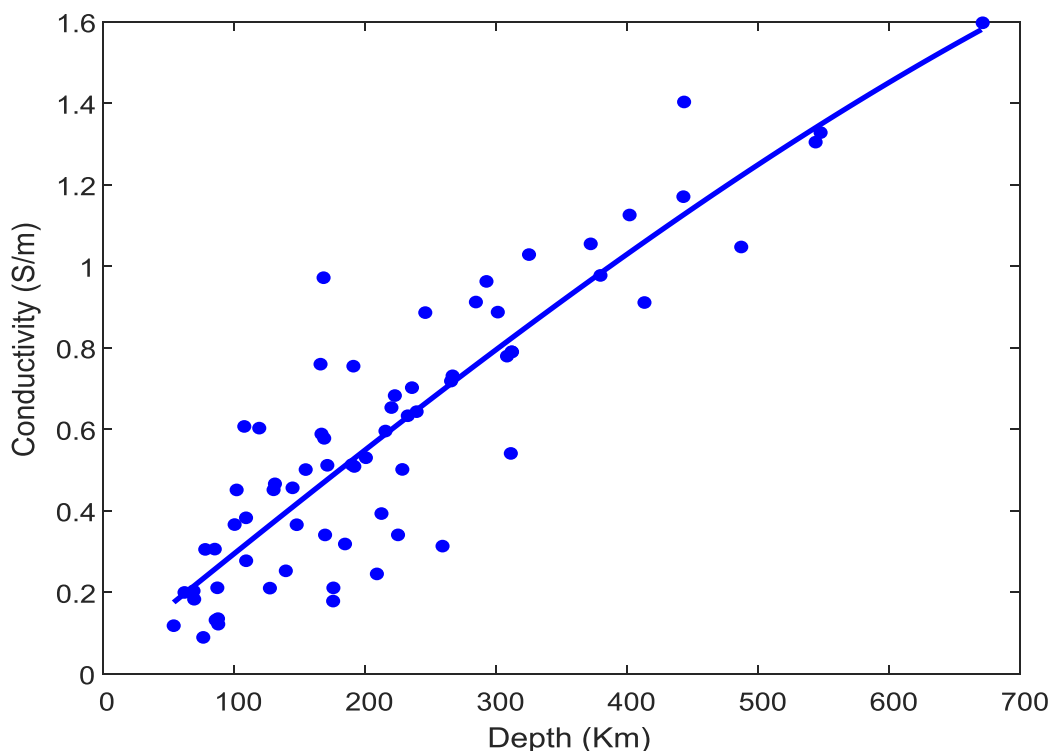


Fig 4: Depth of induction of EEJ to subsurface electrical conductivity at Addis Ababa/Khartoum pair.

Figs 3 and 4 depicts the depth of induction of the equatorial electrojet current to subsurface electrical conductivity profile of the African region based on solar quiet daily variation in the African region. The stations Ilorin (ILR) and Addis Ababa (AAE) represent equatorial latitude while Algeria (AO₂) and Khartoum (KRT) represent off-equatorial stations. The points marked blue represent conductivity values. The conductivity -depth values are represented by the blue solid lines. Generally, the scattered points were found to be more concentrated within the crust and extend up to a depth of about 500 km and with increasing depth, the scattered points decrease. The scattered points observed differs from that reported by [20] who worked in Malaysia and reported sparse concentration of scattered points within the first few kilometers upto 450km and a more concentration of scattered points with increasing depth. "The observed scatter could be attributed to factors such as; error from the field measurements, error from the spherical harmonic analysis

(SHA) fitting, variability of source current locations, and magnetic field contributions from various sources other than the quiet day field" [8]. The error in profiling determination that emanates from noises in the original data and the effect of lateral inhomogeneity are very difficult to evaluate accurately as such what could be regarded as an error is in the measurement of the regression fitting from the scattered conductivity values. Fig 2 and 3 show that the conductivity profiles increases downwards with depth from crustal surface deep down into the lower mantle which conforms with previous work of [21,22,23]. The findings are expected because in the interior of the earth, temperature increases as depth increases thus, the electrical conductivity increases accordingly. The recorded profile obtained for the EEJ at Addis Ababa - Khartoum pair commenced from 0.118S/m at a crustal depth of 54.28km and increased gradually to 0.607S/m at 108.1 km. It decreased to 0.178S/m at 175.88km and increased to 1.054S/m at 325.26km. It continued to

increase and got to 1.403S/m at 443.54km and finally attained a maximum value of 1.597S/m at 671.27km. The profile for the EEJ at Ilorin-Algeria pair started from 0.031S/m at a depth 115.88km, rose steadily 0.04S/m at 159km.,0.063S/m at 285.9km,0.087S/m at 399.76km ,0.099S/m at 414.9km.The profile decline sharply to 0.039S/m at 487.6km and rose sharply again to 0.145S/m at 528.0km.The profile increased steadily till it attained a value of

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0.226S/m at a depth of 726.04km,it declined steadily to 0.169S/m at 837.44km, 0.150S/m at 919.5km.The profile started increasing again till it attained a maximum conductivity of 0.285S/m at 1092km.The increase in conductivity at depth range between 116km to 326km in both profiles correspond to the region of low seismic velocity and high electrical conductivity [20].

CONCLUSION

Naturally slowly time varying geomagnetic daily variation on quiet days(Sqvariation)arising from fluctuating electric current in the ionosphere was used to determine the depth of induction of the equatorial electrojet current to subsurface electrical conductivity in the African region.The following deductions were made from the result:

1. The equatorialelectrojet current penetrates the solid earth upto the lower mantle to about 1092km. depth
2. The electrical conductivity increases downward attaining maximum values in the lower mantle in agreement with global models.
3. Conductivity profiles show conductivities to be about 1.5S/m below 600km, increasing upto about 2S/m at the lower mantle.

4. The rise in conductivity from the crust to about 326km coincides with seismic low velocity layers reported by previous workers.Analysis of Sq(H) variation that incorporates phenomena in the atmosphere (ionosphere) and that of the earth interior using spherical harmonic analysis has been successfully used to profile the conductivity depth structure in the African region. This no doubt will improve on the already existing knowledge of the internal structure and the physical state of the African region. Analysis of a combination of geomagnetic data of solar quiet and disturbed time variation is suggested to have a deeper understanding of the electrical behaviour of the solid earth in the African region.

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